

Problem 17) Changing the variable from x to θ , where $x = \sin^2 \theta$, yields

$$\int_0^1 (x^n / \sqrt{1-x}) dx = 2 \int_0^{\pi/2} \frac{\sin^{2n}(\theta) \sin \theta \cos \theta}{\cos \theta} d\theta = 2 \int_0^{\pi/2} \sin^{2n+1}(\theta) d\theta = 2[(2n)!! / (2n+1)!!].$$
